LARGE TIME BEHAVIOUR OF NEUTRAL DELAY SYSTEMS

MIGUEL VINÍCIUS SANTINI FRASSON

We are interested in *functional differential equations* (FDE) of the form

(1)
$$\begin{aligned} \frac{d}{dt}Mx_t &= Lx_t, \\ x_0 &= \varphi \in \mathcal{C}. \end{aligned}$$

where M and L are linear continuous operators from the space state $\mathcal{C} \stackrel{\text{def}}{=} \mathcal{C}([-1,0],\mathbb{C}^n)$ to \mathbb{C}^n , and $x_t \in \mathcal{C}$ is defined as

$$x_t(\theta) = x(t+\theta), \qquad \theta \in [0,1], \quad t \ge 0.$$

We aim to show a decomposition of the space state $\mathcal{C} \stackrel{\text{def}}{=} \mathcal{C}([-1,0],\mathbb{C}^n)$ as direct sums of $\mathcal{M}_{\lambda} \oplus \mathcal{Q}_{\lambda}$, where \mathcal{M}_{λ} is a finite dimensional subspace of \mathbb{C} , and estimates that reduce the large time behaviour of solutions of the initial value problem (??) to an ordinary differential equation in \mathbb{C}^n .

References

- Miguel V. S. Frasson. Large time behaviour of neutral delay systems. PhD thesis, Leiden University, The Netherlands, 2005.
- [2] Miguel V. S. Frasson and Sjoerd M. Verduyn Lunel. Large time behaviour of linear functional differential equations. *Integral Equations Operator Theory*, 47(1):91–121, 2003.
- [3] Jack K. Hale and Sjoerd M. Verduyn Lunel. Introduction to functional-differential equations, volume 99 of Applied Mathematical Sciences. Springer-Verlag, New York, 1993.
- [4] Sjoerd M. Verduyn Lunel. Spectral theory for delay equations. In Systems, approximation, singular integral operators, and related topics (Bordeaux, 2000), volume 129 of Oper. Theory Adv. Appl., pages 465–507. Birkhäuser, Basel, 2001.

(Miguel V. S. Frasson) DEPARTAMENTO DE MATEMÁTICA APLICADA E ESTAÍSTICA, INSTITUTO DE CIÊNCIAS MATEMÁTICAS E DE COMPUTAÇÃO, UNIVERSIDADE DE SÃO PAULO-CAMPUS DE SÃO CARLOS, CAIXA POSTAL 668, 13560-970 SÃO CARLOS SP, BRAZIL

E-mail address: frasson@icmc.usp.br